

FACULTY OF ELECTRICAL  
ENGINEERING**SUBJECT CARD**

Name in Polish: **Metody numeryczne**  
 Name in English: **Numerical methods**  
 Main field of study (if applicable): **Industrial Control Engineering**  
 Specialization (if applicable):  
 Level and form of studies: **1st level, full-time**  
 Kind of subject: **obligatory**  
 Subject code: **APR012104**  
 Group of courses: **NO**

	Lecture	Classes	Laboratory	Project	Seminar
Number of hours of organized classes in University (ZZU):	15			30	
Number of hours of total student workload (CNPS):	30			60	
Form of crediting:	crediting with grade			crediting with grade	
For group of courses mark (X) final course:					
Number of ECTS points:	1			2	
including number of ECTS points for practical (P) classes :				2	
including number of ECTS points for direct teacher-student contact (BK) classes:	0.70			1.40	

**PREREQUISITES RELATING TO KNOWLEDGE, SKILLS AND OTHER COMPETENCES**

1. Student possesses knowledge of basic mathematical analysis, computer science, linear programming.
2. Student has practical skills in using Matlab software, Matlab programming, testing, debugging and running programs.
3. Student is able to work alone.

**SUBJECT OBJECTIVES**

- C1. Understanding and mastering the basic algorithms of numerical methods  
 C2. Practical skills in the use of basic algorithms of numerical methods in engineering practice

**SUBJECT LEARNING OUTCOMES***relating to knowledge:*

- PEU\_W01 Possesses knowledge related to the representation of numbers in a computer, and types of numerical errors.  
 Possesses knowledge related to the methods for solving systems of linear and non-linear equations.  
 PEU\_W02 Has knowledge of interpolation and approximation of the function.  
 PEU\_W03 Has knowledge related to the numerical algorithms to integration and differentiation of functions, as well as to numerical solution of the differential equations.

*relating to skills:*

- PEU\_U01 Is able to algorithmization and formalization of any engineering task  
 PEU\_U02 Is able to apply the basic algorithms of numerical methods in engineering practice

*relating to social competences:*

- PEU\_K01 Is able to carry out a complex engineering project in a competent way, unaided, undertaking multi-criteria analysis.

## PROGRAMME CONTENT

Form of classes - lecture		Number of hours:
Lec 1	Introduction. Setting rules of course crediting. Issues of representation of numbers in computers. IEEE754 Standard. Correctness of algorithms, computational complexity. Errors of numerical procedures. Gauss elimination method for solving linear equations.	2
Lec 2	Matrix transformations, calculations of determinant and inverse of matrices. Iterative methods of solving linear systems.	2
Lec 3	Solution of nonlinear equations: iterative methods, Aitken's method, bisection method, Newton method and secant method.	2
Lec 4	Systems of nonlinear equations: Newton-Raphson method.	2
Lec 5	Function interpolation: polynomial method. Linear least-squares problems: approximation of functions and data smoothing.	2
Lec 6	Numerical integration methods. Solving of ordinary differential equations. Single and multi-step methods.	2
Lec 7	Stability properties of numerical methods for solving differential equations.	2
Lec 8	Final test.	1
Total hours:		15

Form of classes - project		Number of hours:
Proj 1	Introduction. Setting rules of course crediting. Acquaintance with lab stands and available software. Gauss algorithm to solve systems of linear equations. Using it to the matrix inversion.	2
Proj 2	Gauss-Seidel method to solve a linear system of equations.	2
Proj 3	Solving of nonlinear equations by a simple iteration and Aitken's method.	2
Proj 4	Solving nonlinear equations by Newton's method.	2
Proj 5	Solving of nonlinear equations systems by Newton-Raphson method. Graphical interpretation of solution.	2
Proj 6	Evaluation of the function interpolation by polynomial interpolation method.	2
Proj 7	Evaluation of the function approximation algorithms by the method of least squares with different basis functions.	2
Proj 8	The least square method with singular value decomposition of the matrix.	2
Proj 9	The use of approximation by the least squares method for smoothing and estimation of input data parameters.	4
Proj 10	Algorithms for numerical integration.	2
Proj 11	Rectangles and trapezoids method to solve differential equations - computer simulation of selected dynamic phenomena.	4
Proj 12	Solving of differential equations using system by Runge-Kutta IV-order method on the example of the dynamic simulation of selected dynamical phenomena.	2
Proj 13	Reserve date	2
Total hours:		30

## TEACHING TOOLS USED

- N1. Lecture.  
 N2. Matlab software  
 N3. Project presentation.

## EVALUATION OF SUBJECT LEARNING OUTCOMES ACHIEVEMENT

Evaluation <i>F - forming (during semester) P - concluding (at semester end)</i>	Educational effect number	Way of evaluating educational effect achievement
F1(W)	PEU_W01 PEU_W02 PEU_W03	participation in lectures
F2(W)	PEU_W01 PEU_W02 PEU_W03	final test
P(W)	$P=0,1 \cdot F1 + 0,9 \cdot F2$	
F1(P)	PEU_U01 PEU_U02	activity in classes
F2(P)	PEU_U01 PEU_U02	presentation of the passing projects
P(P)	$P=0,2 \cdot F1 + 0,8 \cdot F2$	

<b>PRIMARY AND SECONDARY LITERATURE</b>
---

<b>PRIMARY LITERATURE:</b>
----------------------------

- |  |
|--|
| <ul style="list-style-type: none"><li>[1] Fortuna Z., Macukow B., Wąsowski J., Metody numeryczne. WNT, Warszawa 2003</li><li>[2] Stachurski M., Metody numeryczne w programie Matlab. Wydawnictwo MIKOM Warszawa 2003.</li></ul> |
|--|

<b>SECONDARY LITERATURE:</b>
------------------------------

- |   |
|---|
| <ul style="list-style-type: none"><li>[1] Jankowscy J. I M., Przegląd metod i algorytmów numerycznych, cz.1, WNT, Warszawa 1981</li><li>[2] Dryja M., Jankowscy J. I M., Przegląd metod i algorytmów numerycznych, cz.2, WNT, Warszaw, 1982</li><li>[3] Kiełbasiński A., Schwetlick H., Numeryczna algebra, WNT, Warszawa 1992</li><li>[4] Krupka J., Morawski R.Z., Opalski L.J., Metody numeryczne dla studentów elektroniki i technik informacyjnych, Oficyna Wydawnicza Politechniki Warszawskiej Warszawa 1999</li><li>[5] Bjorck A., Dahlquist G., Metody numeryczne, PWN, Warszawa 1987</li><li>[6] Baron B., Piątek Ł., Metody numeryczne w C++ Builder. Wydawnictwo Helion 2004</li><li>[7] Mathews J.H., Fink K.D., Numerical methods using MATLAB. Prentice Hall, 2004</li><li>[8] Yang W.Y., Cao W., Chung T.-S., Morris J., Applied Numerical Methods Using MATLAB. Wiley-Interscience, 2005</li></ul> |
|---|

<b>SUBJECT SUPERVISOR</b>
---------------------------

Piotr Pierz, piotr.pierz@pwr.edu.pl
-------------------------------------